Structure and phase transformation of lanthanum chromate

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Lanthanum chromate (LaCrO₄) was synthesized as a low temperature (< 700 °C) intermediate to perovskite-type, lanthanum chromite (LaCrO₃). The lattice parameters, atom positions and bond lengths determined from X-ray powder diffraction show that LaCrO₄ forms a monazite-type crystal structure. Lanthanum chromate forms a solid solution with Ca, having a solubility between 10 and 20 at %. Thermal analysis shows that at ambient oxygen pressure, LaCrO₄ transforms to LaCrO₃ at a temperature near 700 °C. It also indicates that (La, Ca)CrO₄ initially transforms to LaCrO₃ and CaCrO₄ with the subsequent formation of a (La, Ca)CrO₃ solid solution. Evidence of Ca segregation to the surface of (La, Ca) CrO₃ particles is given by Auger electron spectroscopy and scanning electron microscopy.

1. Introduction

Calcium-doped lanthanum chromite (La, Ca)CrO₃ has been considered as an interconnect material for the solid oxide fuel cell. It has an electrical conductivity at 1000 °C ranging from 1 to $60 \, \mathrm{S \, cm^{-1}}$ in a oxygen partial pressure range of 1.013×10^{-15} to $1.013 \times 10^5 \, \mathrm{Pa}$ [1], respectively; and its thermal expansion coefficient can be matched with yttria-stabilized zirconia [2].

In addition to regulating the electrical conductivity and the thermal expansion coefficient, at temperatures within the two phase region (700 °C < T < 1000 °C), Ca exsolves from (La, Ca)CrO₃ with Cr to form low temperature melting compounds from the Ca–Cr–O phase system. These are hereafter referred to as Ca_m(CrO₄)_n (following the notation of Sakai *et al.* [3]). These compounds melt at temperatures as low as 1030 °C and are useful for liquid phase sintering. Studies of these compounds indicate that their compositions depend on the A/B ratio (referring to ABO₃) in (La, Ca)CrO₃ [4], [5].

A necessary condition when using the $Ca_m(CrO_4)_n$ liquid for sintering is that after the densification process, it should dissolve into the (La, Ca)CrO₃ matrix yielding a single phase solid solution. A previous study [6] has shown that the ability to form a solid solution depends on both the solubility of Ca in (La, Ca)CrO₃ as well as the distribution of the liquid phase in the system. If either the volume of the liquid phase is too large, or if it is non-uniformly distributed, the kinetics of dissolution and the solubility limits make it difficult to form a single phase. Consequently, the quantity and uniformity of the exsolved liquid phase must be controlled throughout all the processing steps of (La, Ca)CrO₃. Ideally, one would like to work with a powder in which the transient liquid phase exsolves only during the sintering process and then dissolves into the matrix after densification is complete. Thus for liquid phase sintering, it is desirable to prepare $(La, Ca)CrO_3$ powder which has a homogeneous distribution of phases.

This report summarizes the synthesis and characterization of the crystal structure of pure and Cadoped LaCrO₄. In addition, the Ca solubility is determined and a description is given of the transformation of LaCrO₄ to LaCrO₃, as well as the segregation and distribution of CaCrO₄ in (La, Ca)CrO₃.

2. Experimental procedure

Powders were synthesized as the compositions $LaCrO_4$ and $La_{0.99-x}Ca_xCrO_4$ where x = 0.1, 0.2, 0.3, 0.4. The latter were prepared with an A site deficiency to avoid the formation of unstable Ca excess phases. The notation, $La_{0.99-x}Ca_xCrO_4$ refers to assynthesized compositions. Although the formula indicates a non-stoichiometric composition with respect to the A/B ratio, it is assumed that solid solutions of calcium-doped LaCrO₄ in thermodynamic equilibrium are largely stoichiometric with respect to this ratio (i.e. A/B = 1). Non-stoichiometry within the system is assumed to be manifested in the formation of a second phase. When referring to a stoichiometric solid solution the general notation, $(La, Ca)CrO_4$ is used.

The low temperature liquid mix process [7] was used to synthesize $LaCrO_4$ and $La_{0.99-x}Ca_xCrO_4$. Appropriate amounts of $La_2(CO_3)_3$ and $CaCO_3$ having a nominal purity of 99 at %, were dissolved into a $Cr(NO_3)_3$ solution with the addition of 1 ml deionized water and 0.2 ml nitric acid per gram of dry carbonate. The mixture was heated to ~ 80 °C to dissolve the solids. A 1:1 molar mixture of ethylene glycol (EG) and citric acid (CA) was added to the solution so that the molar ratio of EG:CA:La_{0.99-x}Ca_xCrO₄ = 1:1:1. The solution was then heated to its boiling point (about 90 °C), evolving water and nitrogen oxides. The resulting viscous solution was poured into a preheated ceramic dish in a drying oven at 120 °C. The solution boiled rapidly, producing a foam and then charred. This amorphous char was milled in reagent ethyl alcohol for 8 h to yield a powder from the char residue.

Lanthanum chromate was formed by heating the milled char at a rate of $100 \,^{\circ}\mathrm{C}\,\mathrm{h}^{-1}$ to $550 \,^{\circ}\mathrm{C}$ and holding for 8 h in a flowing argon atmosphere. The argon atmosphere reduced the rate of organic burnoff, thus avoiding the possibility of raising the internal temperatures of the powder above the LaCrO₄ to LaCrO₃ transformation temperature.

The crystallographic data for LaCrO₄ and (La,Ca)CrO₄ were obtained from X-ray powder diffraction (XRD; Model 2000, Scintag Inc.) Specimens were analysed at room temperature using Ni-filtered CuK α_1 radiation, $\lambda = 0.154$ nm. Silicon powder was used as an internal standard. Measurements were collected over the range of 15–60° 2 θ , at 0.03° 2 θ intervals, with a 1 s scan time.

The diffraction pattern corresponded to published data of Manca and Baran [8]. Using their structural model, the lattice parameters were determined by fitting the XRD pattern to the monoclinic system [9, 10]. The model was then refined using a Rietveld analysis program [11]. Initial estimates of the atom positions were taken from CePO₄ data [12]. The XRD data used for Rietveld refinement were collected over the range of 15–100° 20 at 0.03° 20 intervals with a 4s scan time.

Phase transformations were studied using simultaneous differential thermal analysis and thermogravimetric analysis (DTA/TGA; Model 409, Netzsch Inc.) at heating rates of 1 and $10 \,^{\circ}\text{Cmin}^{-1}$ to peak temperatures of 1400 $^{\circ}\text{C}$. Platinum crucibles were used to minimize possible reactions with the powder.

Phase segregation was observed by scanning electron microscopy (SEM; Jeol model T33A). Surface analysis was performed using auger electron spectroscopy (AES; Perkin Elmer model 545) on compacted powders of $La_{0.99-x}Ca_xCrO_3$ where x = 0.1 and 0.3. The perovskite phase was obtained by calcining char powders at 800 °C for 8 h. Specimens were uniaxially pressed at 70 MPa to form a 1.2 cm disc. Specimens sintered at 1400 °C for 2 h were also analysed by AES.

3. Results and discussion

3.1. LaCrO₄ formation

A previous study [13] suggested that perovskite $LaCrO_3$ formed directly from the char when the temperature exceeded 500 °C. However, a preliminary investigation in this study showed that a mixture of

TABLE I X-ray powder diffraction data for LaCrO₄

d _{obs} (nm)	$d_{ m calc}$ (nm)	I/Io _{obs}	hkl
0.5437	0.5439	10	101
0.4955	0.4957	7	110
0.4818	0.4822	7	$01\overline{1}/011$
0.4346	0.4348	17	111
0.4180	0.4180	6	101
0.3617	0.3619/0.3618	16	111/*020
0.3399	0.3401	62	200
0.3233	0.3234	4	002
0.3194	0.3195	100	120
0.3156	0.3158	< 1	$02\bar{1}/021$
0.3077	0.3078/0.3071	16	*210/211
0.2974	0.2976	23	112
0.2952	0.2952	30	$01\overline{2}/012$
0.2719	0.2720	19	202
0.2546	0.2558/0.2546	19	211/*212
0.2501	0.2502	10	112
0.2477	0.2478/0.2475	5	*220/221
0.2423	0.2424	3	122
0.2335	0.2336	3	301
0.2273	0.2274	1	130
0.2260	0.2260	7	031/031
0.2225	0.2227/0.2223	13	$10\overline{3}/31\overline{1}$
0.2182	0.2181	10	221
0.2165	0.2174/0.2164	2	$22\overline{2}/310$
0.2090	0.2089	2	131
0.2046	0.2046	3	312
0.2007	0.2008	32	212
0.1985	0.1986	3	301
0.1967	0.1966	7	231
0.1940	0.1940	30	132
0.1920	0.1921/0.1918/0.1915	15	*320/103/311
0.1852	0.1852	3	023/023
0.1837	0.1837	19	322
0.1808	0.1813/0.1809/0.1809	5	303/*040/231
	0.1805/0.1803		/232/223
0.1789	0.1789	23	132
0.1748	0.1748	12	140
0.1710	0.1710	1	411
0.1696	0.1701/0.1696	9	$400/*40\overline{2}$
0.1655	0.1656/0.1652/0.1651	6	*410/330/412

*These peaks have significantly greater intensities than others in the series.

 $LaCrO_4$ and $LaCrO_3$ often formed at calcination temperatures below 600 °C.

Since it is well known that heat from oxidation of the organic during the liquid mix process raises the internal temperature of the powder several hundred degrees above the furnace temperature, it is likely that the combustion of the organics provided enough heat for partial, if not complete transformation of LaCrO₄ to LaCrO₃, which occurs in the 650 to 700 °C range.

It was found that the circulation of argon in the furnace during calcination greatly reduced the combustion rate of the organics, thereby allowing the actual internal powder temperature to remain below the $LaCrO_4$ to $LaCrO_3$ transformation temperature.

3.2. Crystallographic data

Table I is a summary of the *d*-spacings, relative intensities (I/Io_{obs}) and *hkl* indexing. The observed *d*-spacing (d_{obs}) values generally agree with those reported by Manca and Baran [8]. They concluded that LaCrO₄

TABLE II Crystal data for monoclinic LaCrO₄

Space group	$P2_1/n(C_{2h}^5)$
a (nm)	0.7041(1)
b (nm)	0.7237(1)
c (nm)	0.6693(1)
β	104.94°
V (nm) ³	0.3295
Z	4
$Dx (g cm^3)$	5.138

crystallizes in a monazite-type structure (CePO₄), which belongs to the $P2_1/n$ (C⁵_{2h}) space group.

The present study identified some additional peaks in the diffraction pattern which were not previously recorded. These extra peaks lie in the relative intensity range from 1 to 10%. The calculated *d*-spacings (d_{calc}) were determined from the lattice parameters given in Table II.

The results of Rietvelt refinement are plotted in Fig. 1. The measured data are indicated by points and the refined model is indicated by lines. The narrow plot below the main diagram shows intensity differences between measured and calculated values.

Agreement between the model and observed data can be quantified by the profile (R_p) and weighted profile (R_{WP}) values given by the formulae [14]

$$R_{\rm P} = \frac{\Sigma \left| y_{io} - y_{ic} \right|}{\Sigma y_{io}} \tag{1}$$

$$R_{\rm WP} = \left[\frac{\Sigma w_i (y_{io} - y_{ic})^2}{\Sigma w_i y_{io}^2}\right]^{1/2}$$

where y_{io} is the observed intensity at the *i*th step, y_{ic} is the intensity calculated from the structural model, and w_i is a weight factor given by $(w_i)^{-1} = \sigma_{ip}^2 + \sigma_{ib}^2$. This sum is based on standard deviations associated with the counting statistics of a given peak (σ_{ip}^2) and with the background intensity (σ_{ib}^2) .

In the present investigation, the values determined from the refined data of LaCrO₄ are $R_P = 0.071$ and $R_{WP} = 0.098$.

Table III lists the refined fractional co-ordinates and temperature factors, $B \text{ (nm}^3)$ of the atoms in the LaCrO₄ crystal structure. In this structure, lanthanum is surrounded by nine O atoms; the distances of La–O are 0.119, 0.183, 0.242, 0.242, 0.248, 0.255, 0.264, 0.274 and 0.282 \pm 0.001 nm. Chromium is in a distorted tetrahedral site surrounded by four O atoms. The distances of Cr–O are 0.164, 0.168, 0.170 and 0.172 \pm 0.001 nm. These results agree with a description of the monazite structure in the literature [12].

3.3. Calcium solubility

X-ray diffraction studies on $La_{0.99-x}Ca_xCrO_4$ indicate a solubility limit of $0.1 \le x \le 0.2$. This is approximately the same solubility as in LaCrO₃ [6]. Fig. 2 is a plot of the unit cell volume of monazite-type (La, Ca)CrO₄ versus Ca content. The volume initially decreases with increasing Ca, which is an indication



Figure 1 Top: A comparison of $LaCrO_4$ X-ray powder diffraction data with the $P2_1/n$ structural model. Bottom: Intensity difference between the data and the model. — model; \bullet data.

TABLE III Refined fractional co-ordinates for the atoms in monoclinic LaCrO4

	La	Cr	OI	OII	OIII	OIV
x	0.221(1)	0.198(1)	0.258(2)	0.024(2)	0.373(2)	0.115(2)
у	0.157(1)	0.165(1)	0.002(2)	0.110(2)	0.212(2)	0.336(2)
Z	0.397(1)	0.886(1)	0.079(2)	0.680(2)	0.760(2)	0.011(2)
B(nm ²) ^a	0.0029(4)	0.0058(7)	0.0056	0.0064	0.0062	0.0069

^aB, atomic temperature factor.



Figure 2 Unit cell volume versus Ca content of LaCrO₄ and La_{0.99-x} Ca_xCrO₄ solid solutions, where $0.1 \le x \le 0.4$.

that the smaller Ca ion is replacing La in the structure. However, from 20 to 40 at % Ca, the cell volume is relatively constant. This suggests that Ca has reached its solubility limit. A detailed XRD study revealed the appearance of CaCrO₄ peaks in the 30 and 40 at % Ca compositions.

Calcium chromate crystallizes in a zircon-type structure, which belongs to the I4₁/amd (D_{4h}^{19}) space group [15]. According to Wyckoff [16], the structure is composed of linked Ca^{II}O₄ and Cr^{VI}O₄ tetrahedra. In contrast, the monazite-type LaCrO₄ structure has distorted Cr^VO₄ tetrahedra and La^{III} atoms co-ordinated by nine oxygens. Transformation between the two structures must be reconstructive, since Ca atoms would change from a 4-fold in the zircon-type structure, to a 9-fold co-ordination in the monazite-type structure in forming a solid solution with LaCrO₄. In view of this, it is reasonable that CaCrO₄ would show a solubility limit in LaCrO₄. This is evident from the present results.

3.4. LaCrO₄ phase transformation

X-ray analysis showed that at temperatures above 700°C, the monazite-type structure becomes unstable and transforms to perovskite-type LaCrO₃. This necessarily involves the release of oxygen according to the reaction

$$LaCrO_4 \rightarrow LaCrO_3 + \frac{1}{2}O_2$$
 (2)

The transformation between the two crystal structures is complex and not well understood, but a comparison of the monazite to the perovskite structure [17] shows that La atoms change from a 9-fold to a 12-fold oxygen co-ordination and Cr atoms change from a tetrahedral to an octahedral O coordination. According to electrical neutrality conditions, the Cr atoms are reduced from a +5 to +3 valence, and one O atom per formula unit diffuses out of the bulk crystal to a free surface and is released into the



Figure 3 Combined DTA (—)/TGA (. . . .) data for LaCrO₄. Heating rate, $1 \degree C \min^{-1}$

atmosphere. These crystallographic changes cause a unit cell volume decrease from 0.33 to 0.23 nm³.

The LaCrO₄ to LaCrO₃ transformation was readily observed with DTA and TGA. The DTA/TGA data in Fig. 3 shows the LaCrO₄ to LaCrO₃ transformation occurring at 680 ± 10 °C. The TGA curve yields a weight loss of 6.4 ± 0.1 wt % which agrees with the loss of oxygen (6.3 wt %) predicted by Equation 2. No other interactions or weight changes occurred as the temperature increased to 1400 °C.

When Ca is added to LaCrO₄, the DTA/TGA and XRD results change. The 10 at % Ca composition is single phase in the monazite-type structure and in the perovskite-type structure at temperatures above 800 °C. Since the 10% composition is single phase, it is not interesting in the context of low temperature sintering, so the DTA/TGA study concentrated only on compositions with 20 at % or higher Ca content. For Ca content > 10 at %, thermal analyses showed two endothermic reactions between 600 and 1100 °C, each accompanied with a weight loss.

Figs 4 and 5 illustrate the DTA/TGA analysis of CaCrO₄ and La_{0.99-x}Ca_xCrO₄ with x = 0.2, 0.3 and 0.4. The first reaction between 600 and 700 °C is related to the transformation of LaCrO₄ to LaCrO₃. The transformation temperature shows no systematic behaviour with respect to Ca content. However, TGA behaviour shows decreasing weight loss values at the transformation with increasing Ca content.

X-ray analysis on powders calcined at $800 \,^{\circ}\text{C}$ indicated the formation of a solid solution of Ca in LaCrO₃. Referring to Equation 2 the overall transformation reaction may be written

$$La_{1-u}Ca_{u}CrO_{4} \rightarrow \frac{1-u}{1-v}La_{1-v}Ca_{v}CrO_{3}$$
$$+ \frac{u-v}{1-v}CaCrO_{4} + \frac{1-u}{2(1-v)}O_{2} \qquad (3)$$

where u = 0.2, 0.3, 0.4 and v can be considered as a measure of the initial solubility of Ca in LaCrO₃.

Since oxygen is the only species involved in the weight change, the TGA data may be used to calculate



Figure 4 DTA results of CaCrO₄ and 20, 30 and 40 at % doped lanthanum chromates. Heating rate, $1^{\circ}C \min^{-1}$ —La_{0.79} Ca_{0.2} CrO₄; ---- La_{0.69} Ca_{0.3} CrO₄; ---- La_{0.59} Ca_{0.4} CrO₄; ---- CaCrO₄.



Figure 5 TGA results of CaCrO₄ and 20, 30, and 40 at % doped lanthanum chromates. Heating rate, $1 \,^{\circ}C \min^{-1}$ —La_{0.79} Ca_{0.2} CrO₄; --- La_{0.69} Ca_{0.3} CrO₄; --- La_{0.59} Ca_{0.4} CrO₄; --- CaCrO₄.

v or the solubility of Ca after the transformation. The solubility is calculated by substituting the corresponding values of u and the oxygen loss into the fraction preceding O_2 in Equation 3 and solving for v. Table IV lists the weight loss and v for 20, 30 and 40 at % Ca additions. Within the experimental error of ± 1 at %, the values of v are considered to be zero, which suggests that the amount of dissolved Ca after the transition is negligible. Thus the TGA results imply the (La, Ca)CrO₄ transforms to LaCrO₃ and CaCrO₄ and that Ca does not initially form a solid solution with LaCrO₃.

As the powders are heated to temperatures beyond the transformation temperature, $CaCrO_4$ loses oxygen and dissolves into $LaCrO_3$ to form a solid solution. This is evident by the weight loss after the transformation (Fig. 5).

TABLE IV Solubility, v, of Ca in LaCrO₃ at the phase transformation (600–680 °C), as calculated from thermogravimetric measurements

$\Delta w/w_{o}(\%)$	v		
5.5 ± 0.1	0.00 ± 0.01		
4.8 ± 0.1	-0.04 ± 0.01		
4.5 ± 0.1	0.00 ± 0.01		



Figure 6 An AES depth analysis of a compact of $La_{0.89}Ca_{0.1}CrO_3$ powder. Calcined at 800 °C for 8 h. \Box La; \bullet Ca.

Near 1030 °C, another endothermic reaction accompanied with an increased rate of weight loss is observed. This corresponds to the melting point of CaCrO₄. The melting behaviour of this compound and compositions related to the Ca-Cr-O pseudobinary system has been well characterized [18, 19, 20]. The La_{0.79}Ca_{0.2}CrO₃ composition shows no indication of a reaction, presumably since most of the CaCrO₄ has dissolved into the (La, Ca)CrO₃ matrix before the melting temperature was obtained.

As heating proceeds above the melting point, Ca, Cr, and O continue to dissolve into the $(La, Ca)CrO_3$ matrix. However, the $Ca_m(CrO_4)_n$ liquid also loses weight as indicated by the $CaCrO_4$ curve in Fig. 5. Consequently, the dissolution of Ca, Cr and O into LaCrO₃ can no longer be followed by TGA.

3.5. Calcium chromate distribution

Auger electron spectroscopy (AES) disclosed the formation of a Ca rich surface layer in $(La, Ca)CrO_3$ powder. Figs 6 and 7 show the AES surface profiles of $La_{0.89}Ca_{0.1}CrO_3$ and $La_{0.69}Ca_{0.3}CrO_3$ powders, respectively. These had been calcined at 800 °C for 8 h and pressed into discs. X-ray diffraction showed that the 10 at % Ca composition had formed a single phase, whereas the 30 at % composition had formed a solid solution with excess CaCrO₄. Increased segregation is observed as the Ca content is increased.

Fig. 8 is an AES depth analysis of $La_{0.89}Ca_{0.1}CrO_3$ sintered at 1400 °C. The fact that no excess Ca is observed at the surface indicates a high solubility of Ca and little, if no segregation of CaCrO₄. Similar results are obtained for the 30 mol % Ca composition.



Figure 7 An AES depth analysis of a compact of $La_{0.69}Ca_{0.3}CrO_3$ powder. Calcined at 800 °C for 8 h. \Box La; \bullet Ca.



Figure 8 An AES depth analysis of a $La_{0.89}Ca_{0.1}CrO_3$ disc. Sintered at 1400 °C/2 h. \Box La; \oplus Ca.



Figure 9 A SEM micrograph of a $La_{0.59}Ca_{0.4}CrO_3$ aggregate showing a segregated CaCrO₄ crystal at the top centre. Calcined at 800 °C for 8 h.

X-ray analysis agrees with this, in respect that no $CaCrO_4$ was observed after sintering at 1400 °C.

These observations are related to the solute solubility. When the solubility of Ca in $LaCrO_3$ is low, Ca preferentially segregates to the surface of the primary particle. This becomes evident in AES before it can be detected by XRD. When the solubility of Ca is high, it is stable within the bulk and the surface becomes a homogeneous mixture of La and Ca. A review by Hondros and Seah [21] discusses the theory and phenomenon of surface segregation in detail.

From surface analysis it is concluded that excess Ca will likely segregate to the surface of the (La, Ca)CrO₃ particle within temperature ranges of low solubility. It was also observed by SEM that if homogeneous powders with excess CaCrO₄ are annealed below 1000 °C for a long enough time, the CaCrO₄ will grow on the particle surface and eventually segregate into individual crystals. Such a crystal is evident in the top centre of Fig. 9. If segregation occurs, a non-homogeneous distribution of the Ca_m(CrO₄)_n liquid results. The same distribution of the liquid phase could reduce the effectiveness of sintering or subsequent solid solution formation.

4. Summary

The present investigation has shown that monazitetype $LaCrO_4$ and $(La, Ca)CrO_4$ can be synthesized through the use of the liquid mix process and by calcining in argon at 550 °C. The solubility of Ca in LaCrO₄ is between 10 and 20 at %. When (La,Ca)CrO₄ was heated to ~ 700 °C, intermediate products, LaCrO₃, CaCrO₄ and O₂ evolved. The LaCrO₃ and CaCrO₄ subsequently combined, evolving more O_2 , to form a solid solution, (La, Ca)CrO₃. For powders heated to 800 °C, Ca was seen to segregate to (La, Ca)CrO₃ particle surfaces at low solubility. Scanning electron microscopy showed that crystals of CaCrO₄ segregate from the (La, Ca)CrO₃ particles. Upon heating to 1400 °C, AES showed that 10 and 30 at % Ca compositions regained a homogeneous mixture of La and Ca at the specimen surface, which was an indication that the solubility of Ca in (La, Ca)CrO₃ had increased to form a solid solution.

Acknowledgements

Special thanks is given to Jens Ranløv of Risø National Laboratory for discussions and help with the crystal structure refinement. Financial support was granted in part by Argonne National Laboratories and the division of Basic Energy Science of the US Department of Energy.

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Received 9 February 1994 and accepted 28 April 1995